List the x- and y-intercepts and test for symmetry.

- 9. $x^2 9y^2 = 9$
- 10. How much water must be evaporated from 64 ounces of a 2% salt solution to make a 10% salt solution?

11. A function g is defined by
$$g(x) = \frac{A}{x} + \frac{8}{x^2}$$

If g(-1) = 0, find A.

In problem 12, find the following for each function.

(a)
$$f(-x)$$
 (b) $-f(x)$ (c) $f(x+2)$ (d) $f(x-2)$
12. $f(x) = \frac{x^2}{x+2}$

In problem 13, determine (algebraically) whether the function is even, odd or neither.

13.
$$g(x) = \frac{4+x^2}{1+x^4}$$

In problem 14, find the domain of each function.

$$14. \quad f(x) = \frac{3x^2}{x-2}$$

15. Given: $f(x) = 1 - 3x^2$ and $g(x) = \sqrt{4 - x}$, find: (a) (f \circ g) (2) (b) (g \circ f) (-2) -

In problems 10 to 12, use Descartes' Rule of Signs and the Rational Zeros Theorem to find all real zeros, then use the zeros to factor over the real numbers.

- 10. $f(x) = x^3 x^2 10x 8$
- 11. $f(x) = 4x^3 4x^2 7x 2$

13. (8 - 3i) + (- 6 + 2i)

12. $f(x) = x^4 + 6x^3 + 11x^2 + 12x + 18$

Write each expression in problems 13 to 15 in the form a + bi.

14.
$$\frac{4}{2-i}$$

15. $(3-2i)^3$

In problems 12 and 13, find the exact value of each expression. Do not use a calculator.

12.
$$4 \csc \frac{3\pi}{4} - \cot \frac{-\pi}{4}$$

13.
$$\frac{1}{\cos^2 40^\circ} - \frac{1}{\cot^2 40^\circ}$$

In problem 14, find the exact value of each of the remaining trigonometric functions.

14.
$$\tan A = \frac{-2}{3}, 90^{\circ} < A < 180^{\circ}$$

15. Graph $y = 3 \cos x + 3$

- 10. Find the x- and y-intercepts of $f(x) = \frac{4 x}{x}$, then determine whether the graph of f touches or crosses the x-axis at the x-intercept.
- 11. Solve $3x^4 + 3x^3 17x^2 + x 6 = 0$
- 12. Write 2(1 + i) 3(2 3i) in the form a + bi.
- 13. $F(x) = \sqrt{x-2}$ is one-to-one; find its inverse. Find the domain and range of *f* and *f*⁻¹.
- 14. Write $\log (x^2 9) \log (x^2 + 7x + 12)$ as a single logarithm.
- 15. Find y as a function of x; the constant C is a positive number. $\ln (y 1) + \ln (y + 1) = -x + C$
- 16. Solve $2^{x+1}(8^{-x}) = 4$
- 17. Convert 15º to radians.
- 18. Convert $\frac{2\pi}{3}$ to degrees.
- 19. Find the exact value of $\cos \frac{\pi}{3} + \sin \frac{\pi}{3}$. Do not use a calculator.
- 20. Find the exact value of the remaining trigonometric functions if $\cos A = \frac{-3}{5}$ and $\sin A < 0$.

In problems 10 to 12, find the remaining angle(s) and side(s) of each triangle if it (they) exists. If no triangle exists, say, "No triangle".

- 10. $\alpha = 10^{\circ}$, $\gamma = 40^{\circ}$, side c = 2.
- 11. Side a = 10, side b = 7, side c = 8.
- 12. Side a = 1, side b = 2, $\gamma = 60^{\circ}$.

In problems 13 and 14, find the area of each triangle.

13. Side b = 5, side c = 4, $\alpha = 20^{\circ}$

- 14. Side a = 3, side b = 2 and side c = 2.
- 15. Find the height of a building that is 80 feet away from a point on the ground, when this point on the ground makes an angle of 25° with the top of the building.

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In problem 7, the vector v is represented by the directed line segment PQ. Write v in the form ai + bj or in the form v = a + bj + ck, and find ||v||.

7.
$$P = (-3,1); Q = (4,-2)$$

In problems 8 to 10, identify each equation. If it is a parabola, give its vertex, focus, and directrix; if it is an ellipse, give its center, vertices, and foci; if it is a hyperbola, give its center, vertices, foci, and asymptotes.

8.
$$16x^2 = y$$

9. $\frac{x^2}{9} + \frac{y^2}{16} = 1$
10. $\frac{y^2}{25} - x^2 = 1$

In problem 11, solve the system of equations using substitution or elimination. If the system has no solution, say that it is inconsistent.

11. x - 3y + 5 = 02x + 3y - 5 = 0

In problem 12, find the inverse of the matrix (if there is one) algebraically. If there is not an inverse, say that the matrix is singular.

- 12. |3 1 2| |3 2 -1| |1 1 1|
- 13. Solve the following system using matrices. If the system has no solution, say that it is inconsistent.
 - 2x + y + z = 54x - y - 3z = 18x + y - z = 5

14. Find the determinant of|-40 ||13 |

- 15. Use Cramer's Rule, if applicable, to solve:
 - x 3y = -52x + 3y = 5

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Find the indicated term in each sequence.

- 9. 8th term of 1, -1, -3, -5, ...
- 10. 11th term of 1, 2, 4, 8, ...

Find a general formula for each arithmetic sequence.

- 11. 8th term is -20; 17th term is -47
- 12. 12th term is 30; 22nd term is 50

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10. Write 3 - 2i in polar form.

11. Write
$$4\left(\cos\frac{3\pi}{4} + i\sin\frac{3\pi}{4}\right)$$
 in the standard form $a + bi$.

12. Find *zw* and $\frac{z}{w}$. Leave your answers in polar form.

$$z = 4(\cos 50^\circ + i \sin 50^\circ)$$

 $w = \cos 340^\circ + i \sin 340^\circ$

- 13. Write $(2 2i)^8$ in the standard form a + bi.
- Write v in the form ai + bj or in the form v = ai + bj + ck, and find ||v||.
 P = (4, 7, 0); Q = 0, 5, 6)
- 15. Identify $3y^2 x^2 = 9$. If it is a parabola, give its vertex, focus and directrix. If it is an ellipse, give its center, vertices, and foci. If it is a hyperbola, give its center, vertices, foci and asymptotes.
- 16. Solve the following system of equations using elimination or substitution:

$$2x - y = -1 x + \frac{1}{2}y = \frac{3}{2}$$

17. Find the inverse of |-3 1| |-6 2|

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